

# Surface Water Information Modeling System (SWIMS)

## Gap Tolerance Analysis

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### Executive Summary

#### Purpose

The Oregon Water Resources Department (OWRD) relies on flow duration curves (FDCs) to characterize natural streamflow for water-availability evaluations. This study establishes defensible gap-tolerance criteria—how much missing data can be present while keeping FDCs reliable.

#### Data and scope

We analyzed 51 minimally disturbed index gages with continuous daily records over WY 1991–2020. Gages were selected from low-disturbance HUC-12 watersheds to reflect near-natural hydrologic conditions.

#### Method overview

For each gage, the baseline 30-year FDC was computed from complete data. We then simulated missing data by randomly selecting 15 of the 30 years and removing 10–75% of daily values within those years while retaining all data in the other 15 years (overall retention range: 62.5–95%). Each gap level was iterated 100 times. We compared the mean FDC ( $\pm 1$  SD) to baseline at 20%, 50%, and 80% exceedance. Shannon entropy of monthly flows was used to interpret sensitivity.

#### Key findings

- For the majority of index gages, FDCs remain within  $\pm 15\%$  at key percentiles when  $\geq 80\%$  of the 30-year period is retained ( $\approx 60\%$  completeness within the gapped 15 years, with the other 15 intact).
- Lower-entropy (more skewed) regimes are more sensitive and typically require  $\geq 82.5\text{--}95\%$  overall retention to satisfy the same  $\pm 15\%$  criterion.

#### Program implications for “index gages”

OWRD previously assumed complete records for every year in the 30-year base period. Results indicate that the candidate pool can be expanded to include relatively minimally disturbed gages with less than 30 years of complete record, provided overall retention  $\geq 80\%$  (and higher thresholds for sensitive, low-entropy sites).

#### Recommendations

1. Baseline acceptance: require  $\geq 80\%$  overall retention.
2. Sensitive sites (low entropy): require  $\geq 85\text{--}90\%$  (up to 95%) overall retention.
3. Document entropy (or comparable distribution diagnostics) to flag gages needing stricter thresholds.

These criteria enable broader, defensible use of available records while maintaining FDC integrity for water-availability and related hydrologic analyses.

## Introduction

At the Oregon Water Resources Department (OWRD, referred to as "the Department"), flow duration curves (FDCs) are a fundamental analytical tool for characterizing natural streamflow to support water availability evaluations. FDCs provide critical insight into streamflow variability, which informs resource management decisions, including allocation, conservation, and policy development. Despite their importance, the effect of incomplete streamflow records on FDC accuracy is not well understood, and standardized criteria for allowable data gaps have not been formally established.

This analysis seeks to address these knowledge gaps by determining the maximum percentage of missing data that can be tolerated while preserving the integrity of FDCs. Specifically, FDCs generated from datasets with varying levels of artificially introduced missing data (ranging from 5% to 37.5%) are compared against FDCs derived from complete datasets to identify an acceptable threshold. The analysis identifies a gap tolerance level as the maximum proportion of missing data that results in deviations of no more than 15% from FDCs based on complete data. The findings are based on streamflow data from 51 selected index gages, defined as sites with continuous 30-year mean-daily records (WY 1991–2020) located in minimally impacted watersheds—classified as low or low-to-moderate disturbance in Andrews & Huang (2024).

## Methods

### Data

The analysis utilized mean daily streamflow data from 51 index gages selected for their ability to represent low-disturbance hydrologic conditions. Each gage provides a continuous 30-year record spanning water years 1991 through 2020, ensuring sufficient temporal coverage for robust flow duration curve (FDC) analysis. These gages were strategically chosen to minimize anthropogenic influences and ensure that the streamflow data reflect natural hydrologic conditions, which are essential for accurate and reliable FDC computations.

To achieve this, all selected index gages are situated within minimally impacted HUC 12 sub-watersheds. The degree of anthropogenic disturbance in each sub-watershed was assessed in Andrews and Huang (2024) using a methodology adapted from Falcone et al. (2010, 2011), which incorporates multiple metrics to evaluate human impacts on hydrologic systems. While various disturbance variables were considered, priority was given to avoiding impacts from surface water withdrawals and dam storage. Sub-watersheds were deemed relevant (i.e., low disturbance) if they were classified as low or low-to-moderate disturbance, or if they met the following thresholds: an irrigation withdrawal ratio (ratioed by natural flow estimates using the National Hydrography Dataset [NHDPlus V2.1]) of less than or equal to 0.10 and a

storage ratio (also ratioed by natural flow estimates) of less than or equal to 0.05. This rigorous selection process ensured that the resulting dataset excluded significant hydrologic disruptions, which could otherwise compromise the validity of the FDCs. By focusing on minimally impacted sub-watersheds, the selected data provides a reliable basis for evaluating the sensitivity of FDCs to missing streamflow records and establishing defensible gap tolerance levels.

Table 1. List of index gages with low disturbance.

Station number	Station name	Latitude	Longitude	Basin
13216500	N Fk Malheur R ab Beulah Res nr Beulah, OR	43.948797	-118.172772	Malheur
13331500	Minam R nr Minam, OR	45.61958739	-117.7243687	Grande Ronde
14010000	S Fk Walla Walla R nr Milton, OR	45.829925	-118.170003	Umatilla
14010800	N Fk Walla Walla R nr Milton Freewater, OR	45.885003	-118.201097	Umatilla
14032000	Butter Cr nr Pine City, OR	45.54650278	-119.3049056	Umatilla
14020000	Umatilla R ab Meacham Cr nr Gibbon, OR	45.71874559	-118.3235713	Umatilla
14044000	M Fk John Day R at Ritter, OR	44.88848965	-119.1410902	John Day
14091500	Metolius R nr Grandview, OR	44.62622717	-121.4831067	Deschutes
14074900	Snow Cr nr Sisters, OR	44.116472	-121.662323	Deschutes
14057500	Fall R nr La Pine	43.796484	-121.572753	Deschutes
14055600	Odell Cr nr La Pine	43.575578	-121.881118	Deschutes
14054500	Browns Cr nr La Pine, OR	43.723513	-121.796139	Deschutes
14050000	Deschutes R bl Snow Cr nr La Pine, OR	43.814069	-121.777198	Deschutes
14052500	Quinn R nr La Pine, OR	43.783542	-121.836581	Deschutes
14050500	Cultus R ab Cultus Cr nr La Pine, OR	43.81806	-121.795863	Deschutes
14051000	Cultus Cr ab Crane Prairie Res nr La Pine, OR	43.82094	-121.823488	Deschutes
14052000	Deer Cr ab Crane Prairie Res nr La Pine, OR	43.804606	-121.839252	Deschutes
14097100	Warm Springs R nr Kahneeta Hot Springs, OR	44.85623014	-121.1494931	Deschutes
14096850	Beaver Cr bl Quartz Cr nr Simnasho, OR	44.95789576	-121.3942242	Deschutes
14092750	Shitike Cr at Peters Pasture nr Warm Springs, OR	44.75122815	-121.6331176	Deschutes
14137000	Sandy R nr Marmot, OR	45.39095523	-122.1300863	Sandy
14139800	S Fk Bull Run R nr Bull Run, OR	45.44456683	-122.1095256	Sandy
14138800	Blazed Alder Cr nr Rhododendron, OR	45.45261842	-121.891747	Sandy
14153800	Layng Cr ab Prather Cr nr Disston, OR	43.7092	-122.72757	Willamette
14154500	Row R ab Pitcher Cr nr Dorena, OR	43.73456751	-122.8706253	Willamette
14158500	McKenzie R at Outlet of Clear Lake, OR	44.36095405	-121.9939477	Willamette
14161500	Lookout Cr nr Blue R, OR	44.20984768	-122.2572887	Willamette
14178000	N Santiam R bl Boulder Cr nr Detroit, OR	44.70762303	-122.102573	Willamette
14182500	Little N Santiam R nr Mehama, OR	44.79095516	-122.5795271	Willamette
14187000	Wiley Cr nr Foster, OR	44.37262371	-122.6248055	Willamette
14185000	S Santiam R bl Cascadia, OR	44.391518	-122.5098066	Willamette
14185900	Quartzille Cr nr Cascadia, OR	44.53984671	-122.4359162	Willamette
14210000	Clackamas R at Estacada, OR	45.30039964	-122.3536978	Willamette
14209500	Clackamas R ab Three Lynx Cr, OR	45.12484321	-122.0734113	Willamette
14301000	Nehalem R nr Foss, OR	45.70399837	-123.755404	North Coast
14303600	Nestucca R nr Beaver, OR	45.26621573	-123.8470605	North Coast
14301500	Wilson R nr Tillamook, OR	45.48399439	-123.6901199	North Coast
14301300	Miami R nr Garibaldi, OR	45.575115	-123.874433	North Coast
14306030	Yaquina R nr Chitwood, OR	44.657397	-123.83875	Mid Coast

14305500	Siletz R at Siletz, OR	44.71456114	-123.8862182	Mid Coast
14306500	Alsea R nr Tidewater, OR	44.38817887	-123.8340015	Mid Coast
14306340	E Fk Lobster Cr nr Alsea, OR	44.25012201	-123.6373243	Mid Coast
14316700	Steamboat Cr nr Glide, OR	43.34900889	-122.7289393	Umpqua
14309500	W Fk Cow Cr nr Glendale, OR	42.80455873	-123.6103463	Umpqua
14308000	S Umpqua R at Tiller, OR	42.93040021	-122.9475532	Umpqua
14325000	S Fk Coquille R at Powers, OR	42.89122414	-124.0698188	South Coast
14332000	S Fk Rogue R nr Prospect, OR	42.70790846	-122.3939192	Rogue
14330000	Rogue R bl Prospect, OR	42.72929607	-122.5158717	Rogue
14400000	Chetco R nr Brookings, OR	42.12455317	-124.1870364	South Coast
10396000	Donner Und Blitzen R nr Frenchglen, OR	42.79099436	-118.8674185	Malheur Lake
14118500	W Fk Hood R nr Dee, OR	45.599375	-121.6363611	Hood

## Procedure

The analysis employed a systematic approach to assess the impacts of missing data on flow duration curves (FDCs). The methodology involved the following steps:

### Baseline FDC Computation

FDCs were first generated using the complete dataset for each of the 51 selected index gages, spanning 30 years (water years 1991 through 2020). These uninterrupted daily streamflow records served as the baseline for comparison, providing an accurate representation of natural flow conditions under complete data availability.

### Simulated Missing Data

To evaluate the effects of missing data, subsets of the baseline dataset were created with controlled data gaps. Specifically:

- From the 30-year daily streamflow record, 15 years were randomly selected, and random data gaps of 10–75% were introduced within those selected years.
- All data from the remaining 15 years were retained in full, yielding an overall retention of 62.5–95% of the 30-year record (i.e., 5–37.5% missing).

This approach replicated real-world conditions where missing data occur due to equipment malfunctions, data transmission failures, or other operational challenges. The assumption is that gaps occur randomly throughout the record; however, in practice, gaps may be autocorrelated (e.g., a failing sensor may cause consecutive missing days) or more likely during conditions that stress equipment (e.g., freezing temperatures). These characteristics are not expected to meaningfully influence the results, as both the resampling method and the overall extent of data reduction help minimize the influence of any specific gap pattern.

### Iterative Sampling

To ensure robust results and account for variability, the random sampling and gap-

introduction process was repeated 100 times for each level of missing data (10%, 20%, 30%, etc.). For each iteration, an FDC was computed, yielding a distribution of 100 FDCs for each gap level. This iterative process reduced bias and allowed for a comprehensive evaluation of uncertainty.

## Statistical Analysis

For each level of missing data:

- The mean and standard deviation of the 100 FDCs for each month were calculated to summarize the central tendency and variability.
- The mean FDC  $\pm$  1 standard deviations were compared against the baseline FDC for each month. Note that  $\pm$  1 standard deviations covers 68.3% of the data when assuming normal distribution.
- Deviations were quantified as percentage differences at key exceedance probabilities: 20%, 50%, and 80% of flow duration. These exceedance values were chosen to represent high, median, and low flows, respectively, which are critical for water availability assessments.

## Gap Tolerance Determination

The gap tolerance level was defined as the maximum percentage of missing data at which deviations between the mean FDC (with gaps)  $\pm$  1 standard deviations and the baseline FDC remained within 15% across the evaluated exceedance flows. Generally, a 15% percent bias is considered acceptable for hydrological modelling and 15% change presumptively protective for environmental flows (Moriassi et al, 2007, 2015; Richter et al., 2012). Thus, this threshold reflects an acceptable level of accuracy loss while maintaining the integrity of FDC-based analyses.

## Entropy Analysis

To assess the degree of uniformity in streamflow distributions, Shannon entropy was calculated for each gage and month based on the full (baseline) dataset. Entropy provides a measure of distribution spread—higher entropy indicates a more uniform distribution, while lower values reflect more skewed or peaked distributions. For this analysis, daily streamflow values for each month were binned into 200 equal-width intervals, and the resulting frequency distributions were normalized into probabilities before computing entropy. These entropy values were then used to help interpret the sensitivity of FDCs to missing data, as gages with more uniform flow distributions tended to exhibit higher tolerance to data gaps.

By systematically introducing and evaluating the effects of missing data, this method enabled the identification of robust and defensible gap tolerance levels. The findings provide a clear framework for managing incomplete streamflow records while ensuring reliable FDC computations for water availability and streamflow analysis.

## Results

Table 2 summarizes the minimum data completeness required within the 15 randomly selected years to maintain deviations of  $\leq 15\%$  at the 20%, 50%, and 80% exceedance flow levels. On average, maintaining at least 60% data completeness within these 15 years (equivalent to 20% missing data across the full 30-year period) was sufficient for most index gages to minimize bias in the resulting FDCs relative to those computed from complete datasets. This finding is likely due to the relatively uniform distribution of streamflow observed at many index gages (Figure 1), which makes the FDC less sensitive to random patterns of missing data and reduces the likelihood of significant deviations from the baseline.

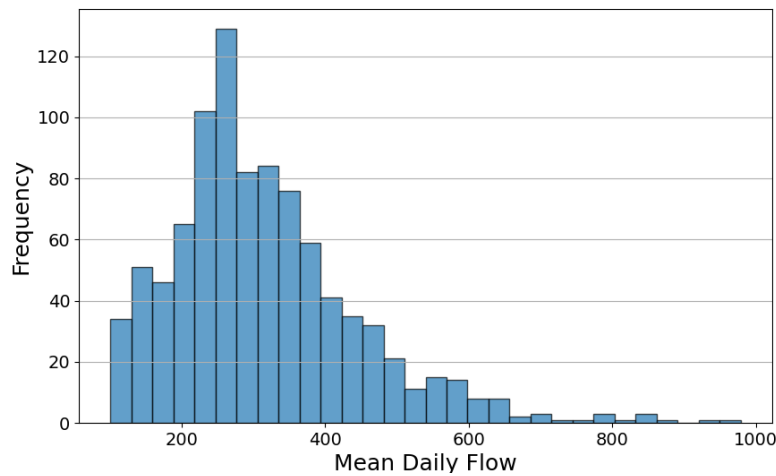


Figure 1. Distribution of mean daily flow data for May from 1991 to 2020 at the gaging station 14010000.

Table 2. Minimum percentage of data needed (within 15 randomly selected years) to represent 20%, 50%, and 80% exceedance flows within a 15% deviation of the full 30-year dataset. The table also includes the corresponding monthly entropy values, which reflect the uniformity of streamflow distributions—with higher entropy indicating more uniform flow patterns across months.

Station	% data	Jan	Feb	Mar	Apr	May	Jun	Jul	Aug	Sep	Oct	Nov	Dec
13216500	50	3.37	3.39	3.87	4.32	4.23	4.27	3.97	3.63	3.44	3.66	3.76	3.24
13331500	35	3.29	3.75	4.07	4.22	4.66	4.64	4.27	4.19	3.86	3.75	3.62	4.03
14010000	<25	3.77	2.69	4.08	4.33	4.51	4.29	4.11	3.63	3.51	3.49	3.84	3.85
14010800	55	3.26	2.30	4.16	3.92	4.27	3.57	3.91	3.99	3.87	2.72	3.53	3.36
14032000	65	2.96	3.42	3.81	3.86	3.83	2.97	3.96	3.56	4.13	4.45	4.20	2.64
14020000	40	3.60	2.65	3.98	4.04	4.30	3.53	4.27	3.99	3.63	2.74	3.53	3.70
14044000	45	3.08	4.04	4.28	4.26	4.08	3.99	3.58	4.37	3.82	4.28	4.24	3.00
14091500	<25	4.08	4.06	4.22	4.11	4.23	4.17	3.87	3.57	3.36	3.50	3.72	4.00
14074900	30	3.44	3.60	3.54	3.83	4.02	3.68	3.89	4.19	4.10	3.84	3.60	3.75
14057500	<25	3.69	3.71	3.72	3.54	3.44	3.35	3.38	3.48	3.48	3.66	3.71	3.71
14055600	<25	4.13	4.31	4.59	4.50	4.72	4.80	4.56	4.27	4.17	4.32	4.38	4.21
14054500	<25	3.21	3.18	3.15	3.17	3.07	3.25	3.36	3.38	3.30	3.31	3.39	3.27
14050000	55	4.46	4.10	4.05	4.23	4.37	4.46	4.72	4.65	4.84	4.84	4.69	4.48
14052500	50	3.35	3.31	3.34	3.36	3.60	3.54	3.62	3.70	3.56	3.39	3.26	3.33
14050500	<25	3.43	3.37	3.40	3.67	4.01	4.02	3.83	3.72	3.94	3.90	3.79	3.69
14051000	90	3.67	3.82	3.82	4.10	4.58	4.72	4.12	4.07	3.04	2.55	2.76	2.67
14052000	90	3.73	3.82	3.97	4.03	4.10	4.09	3.78	3.49	3.24	3.17	3.06	2.88

14097100	40	3.48	3.89	4.08	3.59	4.47	4.48	4.74	4.37	3.79	3.80	3.79	2.90
14096850	50	3.31	3.83	3.96	3.28	3.86	4.26	4.16	3.70	3.47	3.59	4.01	2.16
14092750	<25	3.46	3.74	3.48	3.51	4.23	4.25	4.53	4.67	2.51	2.71	3.24	3.24
14137000	35	3.45	4.05	4.29	3.83	4.40	4.21	4.19	3.96	2.96	2.78	3.61	3.86
14139800	45	3.38	3.88	4.09	3.97	4.35	3.99	4.28	2.75	2.40	3.10	3.42	3.97
14138800	45	3.40	3.70	3.99	3.82	4.16	3.78	3.15	1.95	1.67	2.92	3.48	3.66
14153800	55	3.78	3.79	3.94	2.82	4.15	3.18	3.55	2.78	1.38	2.63	3.16	3.40
14154500	55	3.78	3.88	4.02	3.29	4.13	2.98	3.29	3.37	1.30	2.57	3.22	3.71
14158500	<25	4.24	4.57	4.31	4.40	4.62	4.60	4.57	4.94	4.87	4.37	4.27	4.40
14161500	65	3.42	3.47	3.84	3.42	4.19	3.47	4.25	4.13	1.87	2.40	3.84	3.70
14178000	<25	3.85	3.94	4.17	3.52	4.26	4.17	4.28	4.75	2.82	3.07	3.98	3.85
14182500	55	3.66	3.65	3.96	3.72	4.31	3.68	3.95	2.00	1.65	2.61	3.44	3.86
14187000	60	3.86	4.08	4.22	3.52	4.00	3.16	4.24	3.82	1.24	2.50	3.69	4.20
14185000	65	3.51	3.86	4.24	3.59	4.25	3.52	4.08	3.30	1.50	2.65	3.79	3.79
14185900	65	3.91	3.56	4.07	3.69	4.13	3.55	4.07	2.43	1.15	2.47	3.87	4.08
14210000	30	3.91	4.12	4.25	3.72	4.39	4.12	4.03	4.21	2.64	2.80	3.65	4.00
14209500	<25	3.91	4.12	4.14	3.72	4.33	4.11	4.02	4.35	2.55	2.80	3.64	4.06
14301000	45	4.36	4.07	4.28	4.18	4.04	4.14	4.56	3.25	1.47	2.75	3.90	4.13
14303600	60	4.06	4.15	4.25	4.39	4.47	4.12	4.71	2.98	1.86	2.80	3.77	4.01
14301500	45	4.02	3.79	4.07	3.96	4.17	3.84	4.67	2.65	1.08	2.64	3.54	3.75
14301300	75	3.57	3.89	3.92	4.27	4.15	3.02	4.31	2.70	2.07	3.28	3.33	3.96
14306030	60	3.55	3.86	4.21	4.00	3.91	3.50	4.20	3.98	2.07	2.71	3.41	3.82
14305500	60	3.71	4.09	4.15	4.32	4.20	3.81	4.61	2.95	1.44	2.63	3.57	4.10
14306500	65	3.82	4.11	4.11	3.81	4.22	3.76	4.54	4.03	1.20	2.69	3.59	4.27
14306340	60	3.40	3.45	3.61	3.42	3.89	3.33	4.51	4.04	0.58	2.35	3.47	3.93
14316700	60	3.94	3.98	4.27	3.32	4.30	2.99	3.77	3.91	1.25	2.15	3.50	3.65
14309500	70	3.87	3.18	3.65	3.15	3.63	2.72	4.62	4.62	1.36	1.33	2.72	3.60
14308000	65	3.66	3.76	4.22	3.30	3.90	3.24	4.12	4.45	1.58	2.58	3.43	3.32
14325000	70	3.75	3.55	3.70	3.40	3.55	2.57	4.51	4.84	0.84	1.75	3.19	3.97
14332000	70	2.76	2.81	3.83	3.97	4.38	3.81	3.46	3.78	2.63	3.59	2.82	2.21
14330000	<25	3.97	4.04	4.40	3.95	4.51	4.63	4.55	4.59	4.11	3.91	4.25	3.54
14400000	90	3.93	3.81	3.96	3.21	3.59	2.39	4.61	4.51	0.79	2.01	3.30	4.11
10396000	35	2.52	3.53	3.98	3.97	3.85	4.00	3.65	3.93	4.35	4.18	3.82	2.38
14118500	30	3.78	4.24	3.99	3.97	4.39	4.35	4.04	3.95	2.89	2.84	3.56	3.90

However, certain index gages exhibited lower gap tolerance levels, requiring a minimum of 65-90% data completeness to achieve deviations within the acceptable 15% threshold. The reduced tolerance for these gages is primarily due to their highly skewed streamflow distributions (Figure 2). In such cases, missing data disproportionately affect the FDCs, amplifying deviations and leading to significant biases, particularly at exceedance probabilities dominated by extreme low or high flows.

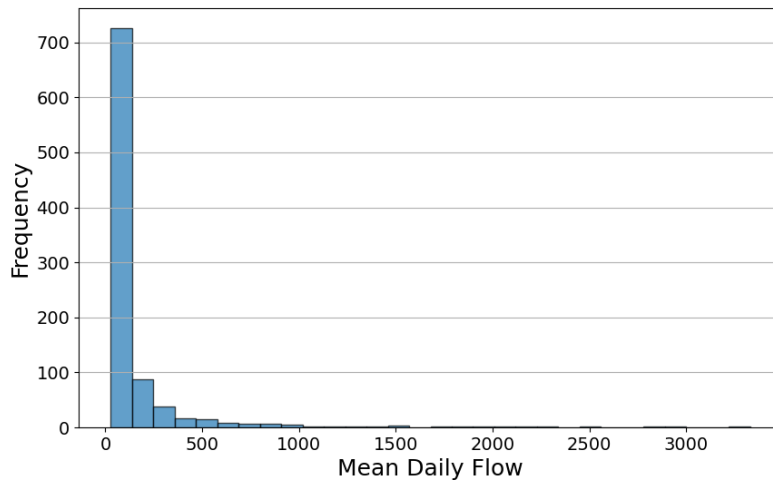


Figure 2. Distribution of mean daily flow data for October from 1991 to 2020 at the gaging station 14325000.

## Discussion

These findings highlight the need to account for streamflow distribution characteristics when determining appropriate gap tolerance levels. Gages with irregular or highly skewed flow distributions—reflected by lower entropy values in Table 2—are inherently more sensitive to missing data, requiring higher levels of data completeness to maintain FDC deviations within acceptable thresholds. In such cases, missing values disproportionately affect key portions of the FDC, especially at exceedance probabilities dominated by extreme low or high flows, amplifying bias. Conversely, gages with higher entropy values, indicating more uniform streamflow distributions, tend to exhibit greater tolerance to data gaps and produce more stable FDCs under conditions of incomplete data. Additionally, the analysis was only applied to minimally disturbed gages for the 1991-2020 base period, and results may not be applicable to disturbed gages or other time periods.

Nevertheless, the analysis confirms that for the majority of index gages, FDCs are relatively robust to missing data, provided that at least 80% of the data is retained across the full 30-year period. In other words, generally, 30-year FDCs at minimally disturbed stations are generally within 15% at key percentiles when at least 80% of daily values are retained — for example, 15 years intact and  $\leq 40\%$  gaps in the other 15 years. Beyond this threshold, deviations from the baseline FDCs become substantial, potentially compromising the reliability of water availability assessments and other hydrologic analyses.

These results show that stations with less-than-perfect data completeness for a period of interest can be useful for characterizing longer-term FDCs, underscoring the importance of setting defensible gap tolerance levels to balance data availability constraints with the need for accurate and reliable FDC computations.

## Conclusion

This study shows that flow duration curves (FDCs) at minimally disturbed Oregon gages are

generally robust to incomplete daily records so long as  $\geq 80\%$  of the full 30-year period (WY 1991–2020) is retained. On average, that standard (equivalent to  $\sim 60\%$  completeness within the 15 randomly sampled years and all data retained in the other 15) keeps deviations at key percentiles within the 15% threshold. Sites with more skewed, low-entropy flow regimes require stricter completeness—typically  $\geq 82.5\text{--}95\%$  overall retention—to meet the same criterion.

We initially assumed each index gage must have complete records for every year of the 30-year base period. These results indicate that the Department can expand the candidate pool to include relatively minimally disturbed gages with less than 30 years of complete record, provided their overall retained data meet or exceed 80% (and higher where flow distributions are highly skewed).

Practically, we recommend a two-tier standard:

1. Baseline acceptance:  $\geq 80\%$  overall retention with no systematic seasonal gaps.
2. Sensitive/low-entropy sites:  $\geq 85\text{--}90\%$  (up to 95%) overall retention.

These findings enable more flexible, defensible use of available records in water-availability evaluations while maintaining FDC integrity. They also highlight where caution is warranted—gages with highly skewed flows.

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